

$$[\underline{A} \underline{I}_s]^* = \underline{A}^* \underline{I}_s^*$$

$$\underline{S}_{3\phi} = \underline{V}_s^T \underline{A}^T \underline{A}^* \underline{I}_s^*$$

$$\underline{S}_{3\phi} = [V_a^0 \ V_a^+ \ V_a^-] \begin{bmatrix} 1 & 1 & 1 \\ 1 & \alpha^2 & \alpha \\ 1 & \alpha & \alpha^2 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 1 & \alpha & \alpha^2 \\ 1 & \alpha^2 & \alpha \end{bmatrix} \begin{bmatrix} I_a^0 \\ I_a^+ \\ I_a^- \end{bmatrix}^*$$

but  $\underline{A}^T \underline{A}^* = 3 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = 3 \underline{U}$  ← unit matrix

$$\underline{S}_{3\phi} = 3 [V_a^0 \ V_a^+ \ V_a^-] \begin{bmatrix} I_a^0 \\ I_a^+ \\ I_a^- \end{bmatrix}^* = 3V_a^0 I_a^{0*} + 3V_a^+ I_a^{+*} + 3V_a^- I_a^{-*}$$

we also know that

$$\underline{S}_{3\phi} = V_a I_a^* + V_b I_b^* + V_c I_c^*$$

EX: The zero and positive sequence components of an unbalanced set of voltages are,

$$V_a^0 = 0.5 - j0.866 \text{ p.u.}$$

$$V_a^+ = 2 \text{ p.u.}$$

$$V_a = 3 \text{ p.u.}$$

obtain the negative sequence component  $V_a^-$  and find the phase voltages,  $V_b$  and  $V_c$ .

$$V_a = V_a^0 + V_a^+ + V_a^-$$

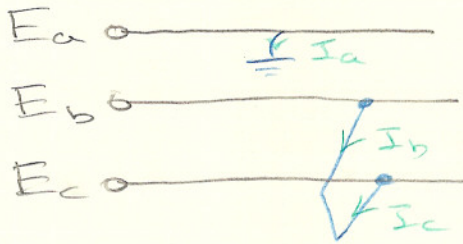
$$V_a^- = 1 \angle 60^\circ$$

$$V_b = V_a^0 + \alpha^2 V_a^+ + \alpha V_a^- = 3 \angle -120^\circ$$

$$V_c = V_a^0 + \alpha V_a^+ + \alpha^2 V_a^- = 0 \quad 120^\circ$$

Fault: a single line to ground on phase C.

Ex:



simultaneous faults.

Obtain the sequence network connection

SOL:

$$\left. \begin{array}{l} I_b + I_c = 0 \\ V_a = 0 \\ V_b = V_c \end{array} \right\} \text{given}$$

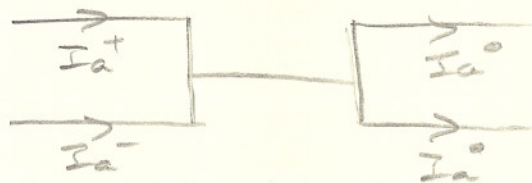
$$I_a^+ = \frac{1}{3} [I_a + (\alpha - \alpha^2) I_b]$$

$$I_a^- = \frac{1}{3} [I_a + (\alpha^2 - \alpha) I_b]$$

$$I_a^0 = \frac{1}{3} [I_a]$$

$$\therefore I_a^+ + I_a^- = 2 I_a^0$$

which can be represented by

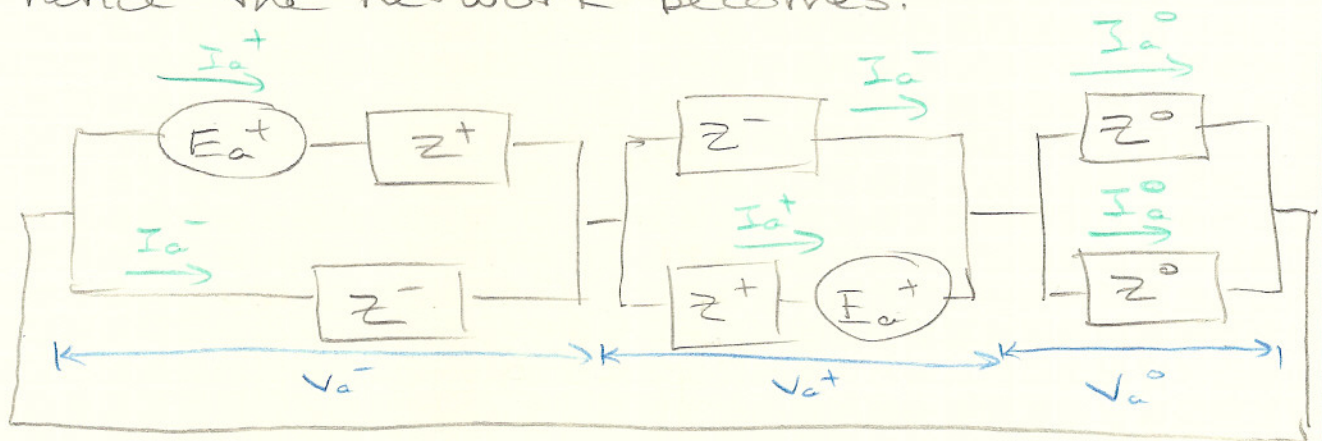


$$V_a^+ = \frac{1}{3} [(\alpha + \alpha^2) V_b] = -\frac{1}{3} V_b$$

$$V_a^- = \frac{1}{3} [(\alpha + \alpha^2) V_b] = -\frac{1}{3} V_b$$

$$V_a^0 = \frac{1}{3} [2 V_b]$$

since  $V_a^+ = V_a^-$  and  $V_a^0 + V_a^+ + V_a^- = V_a = 0$   
hence the network becomes.



## POWER SYSTEM STABILITY

Here we are concerned with the implications of a major network disturbance such as a short circuit, open circuit, or the switching on of a major load. we are interested in how the system behaves following a disturbance.